

LPS 241: Foundations of Classical Field Theory

Winter & Spring 2017

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Lectures: Tu/Th 3:30pm-4:50pm in SSL 171
Office Hours: Th 11:00am-12:00pm

Description: This two-quarter sequence will provide an introduction to differential geometry and classical field theory, including general relativity and Yang-Mills theory. If time permits we will also cover the geometrized formulation of Newtonian gravitation or other special topics, depending on class interest. Our presentation will differ from a course on these topics offered in a physics or mathematics department in that the emphasis throughout will be on the “foundations” of these physical theories. Some specific topics to be covered will include the logical structure of the theories; the geometrical significance of Einstein’s equation, the Yang-Mills equation, and “gauge” potentials; the status, interpretation, and relations between various principles of symmetry and conservation; the causal and topological structure of spacetime; and the relationships between general relativity and theories of force and matter.

Prerequisites: Though there are no formal prerequisites for this course, I will take for granted a background in basic undergraduate mathematics and physics, including calculus in several variables, linear algebra, point-set topology, abstract algebra, special relativity, and Newtonian gravitational theory.

Course Website: <https://eee.uci.edu/17w/66730> (password: kretschmann)

Course Texts:

Topics in the Foundations of General Relativity and Newtonian Gravitation Theory, by David B. Malament.

Classical Field Theory Lecture Notes (available online).

Notes on Reading: Much of the course will follow Malament’s book closely (with some minor rearrangement). However, I will supplement it in some places to discuss additional topics. In these instances, my presentation will follow my Classical Field Theory Lecture Notes. This latter document is constantly evolving, but I will alert you when I make significant changes. A bibliography of supplementary texts will be maintained on the course website; in cases where these are available online, they will be linked to.

Requirements: Auditors are welcome; all that is required for an S is regular attendance and occasional participation. If you would like a grade, you will need to submit written work. The requirements for the first quarter will be problems from Malament (2012) and from my lecture notes, as I will describe in class. For the second quarter, the requirement will be a ~10-15 page paper, the topic of which will need to be approved in advance. (Ideally, we will work closely on the paper before you submit it.)

Collaboration: You are encouraged to collaborate on the problem sets, though everyone needs to produce his or her own write-up. I prefer typed problem sets and value careful presentations that show your work. (Learn Latex.) If you do collaborate, you should indicate as much on top of the problem set before turning it in. Also, while working on the problems, please feel free to talk with me as much as you like.

Course Schedule: The basic structure will be that the first quarter will be devoted to mathematical topics in differential geometry and the second quarter will be devoted to general relativity, classical Yang-Mills theory, and other special topics. A more precise (though still-rough) outline is below; however, I do not intend to force the pace of the course to stick to a particular schedule and so we may cover a sub- or superset of these topics.

Winter Quarter

Week 1

Tuesday Introduction; manifolds
Thursday Manifolds (cont.); smooth maps and diffeomorphisms

Week 2

Tuesday Tangent vectors
Thursday Vector fields and integral curves

Week 3

Tuesday Covectors and tensor fields
Thursday Covectors and tensor fields (cont.)

Week 4

Tuesday **No class**
Thursday **No class**

Week 5

Tuesday Pushforward and pullback maps; submersions and immersions; submanifolds
Thursday Fiber bundles

Week 6

Tuesday Bundle morphisms; cross sections and lifts
Thursday Lie derivatives; Covariant derivative operators

Week 7

Tuesday Covariant derivative operators (cont); exterior derivatives
Thursday Ehresmann connections

Week 8

Tuesday Parallel transport and holonomy
Thursday Curvature

Week 9

Tuesday Metrics
Thursday Metrics (cont.); metric submanifolds; volume elements

Week 10

Tuesday Lie groups and Lie algebras
Thursday Principal and associated bundles

Week 11

TBD Connections and curvature on principal bundles

Spring Quarter

Week 1

Tuesday Relativistic spacetimes; temporal orientation and causal connectivity
Thursday Proper time; space-time decomposition; particle dynamics

Week 2

Tuesday The energy-momentum field
Thursday Einstein's equation

Week 3

Tuesday Fluids
Thursday FLRW Spacetimes

Week 4

Tuesday Killing fields & conserved quantities
Thursday Electromagnetic fields

Week 5

Tuesday Electromagnetic fields (cont.)
Thursday Yang-Mills fields

Week 6

Tuesday Matter fields
Thursday Lagrangian field theory

Week 7

Tuesday Lagrangian field theory
Thursday **No class**

Week 8

Tuesday Hyperbolic systems
Thursday **No class**

Week 9

Tuesday Hyperbolic systems
Thursday Initial value formulation

Week 10

Tuesday Classical Spacetimes
Thursday Geometrized Newtonian Gravitation